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Non-centrosymmetric Ba₃Ti₃O₆(BO₃)₂

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Abstract

The compound previously reported as $Ba_2Ti_2B_2O_9$ has been reformulated as $Ba_3Ti_3B_2O_{12}$, or $Ba_3Ti_3O_6(BO_3)_2$, a new barium titanium oxoborate. Small single crystals have been recovered from a melt with a composition of $BaTiO_3:BaTiB_2O_6$ (molar ratio) cooled between 1100°C and 850°C. The crystal structure has been determined by X-ray diffraction: hexagonal system, non-centrosymmetric $P\bar{6}2m$ space group, a = 8.7377(11) Å, c = 3.9147(8) Å, Z = 1, $wR(F^2) = 0.039$ for 504 unique reflections. Ba_3Ti_3O_6(BO_3)_2 is isostructural with K₃Ta₃O₆(BO₃)₂. Preliminary measurements of nonlinear optical properties on microcrystalline samples show that the second harmonic generation efficiency of $Ba_3Ti_3O_6(BO_3)_2$ is equal to 95% of that of LiNbO₃. © 2003 Elsevier Inc. All rights reserved.

Keywords: Ba3Ti3O6(BO3)2; Ba3Ti3B2O12; Crystal structure; NLO properties

1. Introduction

The discovery, synthesis and crystal chemistry of new inorganic borates with potentially useful optical properties is of continuing interest [1–5]. Recent investigations by our group of ternary systems of the type $MO-M'_2O_3$ - B_2O_3 (M = Sr, Ba, Pb; M' = Al, Ga, Fe, Mn) have led to the discovery of two new borate structure types including $MGa_2B_2O_7$ [6] and $PbM'BO_4$ [7,8]. These compounds are centrosymmetric and have no secondorder nonlinear optical (NLO) properties but some of them, such as PbMnBO₄, display unusual one-dimensional magnetic properties [9]. In this work, attention is focussed on the BaO-TiO2-B2O3 system in which previous studies have identified two ternary compounds: dolomite-type BaTiB₂O₆ [10,11] and a compound reported as Ba₂Ti₂B₂O₉ that could not be synthesized in pure form [12]. A search of the ICDD database [13] revealed that the hexagonal unit-cell determined for $Ba_2Ti_2B_2O_9$ (a = 8.721 Å, c = 3.933 Å) was in fact very similar to the unit-cells of the non-centrosymmetric borates, $K_3Ta_3O_6(BO_3)_2$ (a = 8.781 Å, c = 3.899 Å) [14,15] and the high-temperature form of K₃Nb₃O₆ $(BO_3)_2$ (*a* = 8.779 A, *c* = 3.983 A) [16]. This observation

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suggested that "Ba₂Ti₂B₂O₉" should be re-formulated as Ba₃Ti₃B₂O₁₂, or more precisely Ba₃Ti₃O₆(BO₃)₂. Our results confirm the correct composition of this new barium titanium oxoborate and contradict a very recent survey of the BaO–TiO₂–B₂O₃ system [35] in which the incorrect "Ba₂Ti₂B₂O₉" composition was again reported. The synthesis and structure determination of Ba₃Ti₃O₆(BO₃)₂ are presented here together with the preliminary measurements of its NLO properties.

2. Solid-state synthesis and crystal growth

Polycrystalline samples of $Ba_3Ti_3O_6(BO_3)_2$ were synthesized by solid-state reactions of stoichiometric amounts of $BaCO_3$ (99%, J.T. Baker) or $Ba(NO_3)_2$ (99%, Alfa Aesar), TiO₂ (99.9%, Cerac) and B(OH)₃ (99.99%, Alfa Aesar). After dehydration of boric acid by slow heating to 500°C, 0.5 g pellets were heated up to 900°C for several days with several intermediate remixings. The reaction products were analyzed by powder X-ray diffraction (Guinier-Hägg camera, CuK α_1 radiation, Si internal standard). In all syntheses, a minor or trace amount of BaTiO₃ perovskite was identified in the products, even after prolonged heating of a sample for 10 days at 900°C. This was likely the result of a slight loss of B_2O_3 by evaporation at high temperature since

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addition of a small excess of B(OH)₃ (10 mol%) to the starting mixture eliminated BaTiO₃ from the products and led to the formation of some $BaTiB_2O_6$ instead. The synthesis was also carried out using starting mixtures containing either stoichiometric amounts of BaTiO₃ perovskite (99.99%, Aldrich) and B(OH)₃, or stoichiometric amounts of BaTiO₃ and pre-reacted BaTiB₂O₆. A trace amount of perovskite was present in the products of these reactions as well. Overall, it was observed that either BaTiO₃ or BaTiB₂O₆ formed more readily than $Ba_3Ti_3O_6(BO_3)_2$ which only appeared in the products of solid-state reactions for temperatures above 800°C. This observation is in agreement with the results of our crystal growth experiments in which crystals of BaTiO₃ and BaTiB₂O₆ were more readily obtained than crystals of $Ba_3Ti_3O_6(BO_3)_2$. The possibility that $Ba_3Ti_3O_6(BO_3)_2$ is thermodynamically stable at high temperature only has not been further investigated in this work.

As noted by previous authors for the hypothetical Ba₂Ti₂B₂O₉ compound [12], Ba₃Ti₃O₆(BO₃)₂ was found to melt incongruently at temperatures above 950°C. Therefore, crystallization experiments were carried out by slowly cooling melts of various compositions intermediate between BaTiO₃ and BaTiB₂O₆, and the best results were obtained by using a 1:1 mixture (molar ratio). A 12 g sample was melted at 1100°C in a covered platinum crucible, held at that temperature for 3h, cooled to 850° C at 1° C h⁻¹ and quenched in air. The crystallization products consisted of colorless hexagonal plates of BaTiB₂O₆ as the major phase, together with light yellow blocky crystals of tetragonal BaTiO₃ and light green-yellow prisms of BaTi₂O₅, plus small colorless hexagonal plates of $Ba_3Ti_3O_6(BO_3)_2$. Because the latter were difficult to distinguish from the BaTiB₂O₆ plates under the optical microscope, suitable single crystals of Ba₃Ti₃O₆(BO₃)₂ were identified by determining their unit-cell parameters with a single-crystal diffractometer.

Unsuccessful attempts were made to extend the crystal chemistry of the Ba₃Ti₃O₆(BO₃)₂ structure-type via substitution of the Ba²⁺ and/or Ti⁴⁺ cations, as suggested by the isostructural relationship with $K_3M_3B_2O_{12}$ (*M*=Ta, Nb) [14–16]. For example, although dolomite-type $BaSnB_2O_6$ exists [1] and can be readily synthesized by solid-state reactions, Ba₃Sn₃ B₂O₁₂ could not be synthesized in our experiments, which yielded a mixture of BaSnO3 and BaSnB2O6 instead. Similarly, only perovskite-type phases were recovered in the attempted syntheses of Pb₃Ti₃B₂O₁₂, $Pb_3Sn_3B_2O_{12}$ and $Sr_3Ti_3B_2O_{12}$. Finally, the formation of a solid solution between the isostructural Ba₃Ti₃O₆ (BO₃)₂ and K₃Ta₃O₆(BO₃)₂ compounds was investigated by solid-state reactions of either unreacted starting materials or pre-reacted end-members. Surprisingly, only very limited solid solution (5-10% at most) was found to form at either end of the $Ba_3Ti_3O_6(BO_3)_2$ - $K_3Ta_3O_6(BO_3)_2$ system. Complex oxide compounds formed instead with, for instance, a compound closely related to $Ba_3Ti_4Ta_4O_{21}$ [17] forming as the major phase in a 1:1 mixture of pre-reacted end-members heated up to 900°C for several days.

3. Structure determination

The structure of $Ba_3Ti_3O_6(BO_3)_2$ was determined by single-crystal X-ray diffraction using intensity data collected on a Bruker P4 diffractometer equipped with a MoKa rotating anode X-ray source and a SMART 1K CCD area detector. The raw intensity data were first corrected for Lorentz and polarization effects with the computer software SAINT [18] and an empirical absorption correction was then applied using the program SADABS [19]. The details of the crystal data and the refinement procedure are given in Table 1. The structure solution was obtained in the non-centrosymmetric hexagonal space group $P\bar{6}2m$ with the programs SHELXS [20] and SHELXL97 [21]. The lack of a center of symmetry was confirmed by observing a second harmonic generation (SHG) signal using a polycrystalline sample (initial test performed by A. Kahn-Harari at Ecole Nationale Supérieure de Chimie de Paris, France-see also below). The full least-squares refinement of 27 parameters was then carried out with anisotropic displacement parameters for all atoms, a secondary extinction parameter and a chiral twin parameter (refined to 0.04(4) indicating that the crystal

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Crystallographic data and refinement details for Ba₃Ti₃O₆(BO₃)₂

Crystal system	Hexagonal		
Space group	$P\bar{6}2m$		
Unit-cell parameters (Å)	a = 8.7377(11)		
	c = 3.9417(8)		
Unit-cell volume (Å ³)	260.62		
Z	1		
Calc. density $(g cm^{-3})$	4.902		
Wavelength	ΜοΚα		
Crystal dimensions (mm)	0.15 imes 0.20 imes 0.30		
Absorption coefficient (mm^{-1})	13.40		
$2\theta \max (\text{deg})$	72.61		
Index ranges	-13 < h < 14		
-	-14 < k < 11		
	-5 < l < 6		
Unique reflections	504		
Absorption correction	SADABS		
T_{\min}/\hat{T}_{\max}	0.599		
BASF (chiral twinning parameter)	0.04(4)		
R _{int}	0.036		
Refined parameters	27		
Goodness-of-fit	1.208		
$R[F > 4\sigma(F)]$	0.016 (for 493 reflections)		
$wR(F^2)$	0.039		
Difference map $(e Å^{-3})$	1.04 (1.38 Å from Ba)		
	-1.00 (0.74 Å from Ba)		

Table 2 Atomic coordinates and equivalent isotropic displacement parameters for $Ba_3Ti_3O_6(BO_3)_2$

Atom	X	у	Ζ	$U_{ m eq}({ m \AA}^2)$		
Ва	0	0.60021(4)	1/2	0.00860(9)		
Ti	0	0.23664(11)	0	0.0087(2)		
В	2/3	1/3	0	0.0057(10)		
O ₁	0	0.2606(6)	1/2	0.0168(9)		
O_2	0	0.8103(4)	0	0.0076(6)		
O ₃	0.6778(5)	0.4942(5)	0	0.0197(7)		
(a) Anisotro	pic displacement param	eters for $Ba_3Ti_3O_6(BO_3)_2$	Um	Um	U ₁₂	Un
		0.22	0,00,00(1)	C 23	0 15	
Ba	0.0099(2)	0.0086(1)	0.0078(1)	0	0	0.00497(7)
Ti	0.0030(4)	0.0036(3)	0.0193(4)	0	0	0.0015(2)
В	0.004(2)	0.004(2)	0.009(2)	0	0	0.0021(8)
O_1	0.017(2)	0.014(1)	0.020(2)	0	0	0.008(1)
O_2	0.005(2)	0.005(1)	0.013(1)	0	0	0.0023(8)
0 ₃	0.014(2)	0.008(1)	0.039(2)	0	0	0.007(1)

Table 3

Bond distances (*l*), bond valences (*s*) and bond valence sums $(\sum s)$ in Ba₃Ti₃O₆(BO₃)₂

	<i>l</i> (Å)	s (observed) ^a	s (predicted) ^b
Ba–O1	2.968(5)	0.160	0.185
Ba–O1 \times 2	3.071(1)	0.121	0.185
Ba–O2 \times 2	2.693(3)	0.336	0.203
$Ba-O3 \times 4$	2.909(3)	0.188	0.130
$Ba-O3 \times 4$	$3.172(3)^{c}$	0.092	0.130
$\sum s$		2.19	2.00
$Ti-O1 \times 2$	1.9819(7)	0.637	0.722
$Ti-O2 \times 2$	1.896(1)	0.803	0.797
$Ti-O3 \times 2$	2.081(3)	0.487	0.481
$\sum s$		3.85	4.00
$B-O3 \times 3$	1.360(3)	1.030	1.000
$\sum s$		3.09	3.00
O1–Ba	2.968(5)	0.160	0.185
$Ba \times 2$	3.071(1)	0.121	0.185
$Ti \times 2$	1.9819(7)	0.637	0.722
$\sum s$		1.68	2.00
$O2-Ba \times 2$	2.693(3)	0.336	0.203
Ti imes 2	1.896(1)	0.803	0.797
$\sum s$		2.28	2.00
$O3-Ba \times 2$	3.172(3)	0.092	0.130
$Ba \times 2$	2.909(3)	0.188	0.130
Ti	2.081(3)	0.487	0.481
В	1.360(3)	1.030	1.000
$\sum s$		2.08	2.00

^aCalculated using the equation $s_i = \exp[(r_0 - r_i)/0.37]$ introduced by Altermatt and Brown [27] and the r_0 bond valence parameters of Brese and O'Keeffe [34].

^bPredicted using the method described by O'Keeffe [28,29].

 $^{\rm c}$ The next Ba–O distance is 4.479 Å with a negligible bond valence of 0.003 v.u.

used was essentially untwinned). The refinement converged to $wR(F^2) = 0.039$ for 504 unique reflections. The atomic positions and equivalent isotropic tempera-

ture parameters for $Ba_3Ti_3O_6(BO_3)_2$ are given in Table 2, and the anisotropic displacement parameters are listed in Table 2a. The bond distances and the corresponding bond valences and bond valence sums are listed in Table 3.

The anisotropy observed for the U parameters of the Ti and O3 atoms (Table 2a) led us to attempt the structure refinement in two subgroups of $P\bar{6}2m$, namely P31m and $P\bar{6}$. These refinements, however, did not produce any significant improvement and furthermore indicated the presence of additional two-fold axes perpendicular to the *c*-axis in P31m, or mirror planes parallel to the *c*-axis in P - 6. It was therefore concluded that the Ba₃Ti₃O₆(BO₃)₂ structure is best described in the same $P\bar{6}2m$ space group symmetry as K₃Ta₃O₆(BO₃)₂ [15] and the high-temperature form of K₃Nb₃O₆(BO₃)₂ [16].

4. Description and bond valence analysis of the $Ba_3Ti_3O_6(BO_3)_2$ structure

The structure is illustrated in Fig. 1. It consists of trimers of corner-sharing TiO₆ octahedra which are interconnected by BO₃ groups to form (001) layers. These layers are linked in the c direction by the apical O₁ atoms of the TiO₆ octahedra to create a three-dimensional Ti₃B₂O₁₂⁻⁻ framework with [001] triple octahedral chains. The Ba²⁺ cations are located in irregular pentagonal tunnels parallel to the *c*-axis and their coordination can be described as a tricapped pentagonal prism by including all the Ba–O bonds up to 3.17 Å (Table 3). Similar coordination environments occur in the isostructural borates K₃M₃O₆(BO₃)₂ (M=Ta, Nb) [14–16,22] and in the related silicates Ba_{1.5}Nb₃O₆(Si₂O₇) and K₃Nb₃O₆(Si₂O₇) [23–26].

The bond valence analysis of the $Ba_3Ti_3O_6(BO_3)_2$ structure yields adequate bond valence sums with only



Fig. 1. View of the $Ba_3Ti_3O_6(BO_3)_2$ structure projected on the (001) plane of the hexagonal unit cell. The off-center displacement of the Ti⁴⁺ cations has been illustrated for one of the TiO₆ octahedra.

minor deviations from their expected values except for the O₁ and O₂ atoms which are significantly underbonded ($\sum s = 1.68$) and overbonded ($\sum s = 2.28$), respectively (Table 3). The bond valences expected from the bond topology of the Ba₃Ti₃O₆(BO₃)₂ structure have also been calculated using the method described by O'Keeffe [28,29]. In this method, the valences of individual bonds are predicted by solving a system of equations expressing the bond valence sum rule at the "cation" and "anion" sites and the connectivity, or bond topology, within a crystal structure. For the Ba₃Ti₃O₆(BO₃)₂ structure, the comparison of the observed and predicted bond valences (Table 3) leads to the following conclusions:

- (i) The distortion of the TiO_6 octahedra is mostly a result of the bond topology as shown by the correct prediction of different bond valences for the Ti-O bonds, increasing in the order Ti-O3 < Ti-O1 < Ti-O2 with a wide spread of valences from 0.48 to 0.80 valence units (v.u.) (Table 3). In particular, the large difference between the short Ti-O2 and long Ti-O3 bonds (associated with the 0.2 Å off-center shift of the Ti^{4+} cations in the TiO_6 octahedra—Fig. 1) is well predicted by the bond valence analysis. Similar octahedral distortions are present in K3Ta3O6 $(BO_3)_2$ [6] and $K_3Nb_3O_6(BO_3)_2$ [7] and can also be attributed to the bond topology of that particular structure type. The slight underbonding of the Ti site arises from the stretching of the Ti-O1 bonds $(s_{\text{observed}} = 0.64 \text{ v.u. vs. } s_{\text{predicted}} = 0.72 \text{ v.u.})$ which must be due to non-bonded interactions, such as $Ba^{2+} \cdots Ti^{4+}$ repulsions.
- (ii) The underbonding of the O1 position is due to the systematic stretching of the Ti–O1 and Ba–O1 bonds (with smaller bond valences than predicted),

whereas the overbonding of the O2 atom is due mainly to the compression of the Ba-O2 bonds (with a larger bond valence than predicted) (Table 3). The $Ba_3Ti_3O_6(BO_3)_2$ structure contains, therefore, both tensile and compressive residual bond strain which cannot be easily relieved: as seen in Fig. 1, the Ba-O1 bonds cannot be shortened without also shortening the already compressed Ba-O2 bonds. The bond strain can be quantified by calculating the index $R = \langle (V_i - \sum s_{ij})^2 \rangle^{1/2}$ equal to the root-mean square of the bond-valence sum deviations, with V_i and $\sum s_{ij}$ representing the oxidation state and the bond valence sum of atom *i*, respectively [30]. For $Ba_3Ti_3O_6(BO_3)_2$, R = 0.19 v.u. (with major contributions from the bond valence sums around the O1 and O2 atoms-Table 3), close to the limiting value of 0.2 v.u. which has been proposed as an indicator of instability of a crystal structure and of the possible occurrence of phase transitions [30,31]. Apart from the slight anisotropy in some of the atomic displacement parameters mentioned above, no indication of a phase transition of the type reported in K₃Nb₃O₆ $(BO_3)_2$ [16,22] has been observed in the present study of $Ba_3Ti_3O_6(BO_3)_2$. Nevertheless, the presence of bond strain in its crystal structure may well play a role in its apparent marginal stability by comparison with $BaTiO_3$ and $BaTiB_2O_6$.

5. Measurement of nonlinear optical (NLO) properties

The efficiency of SHG in $Ba_3Ti_3O_6(BO_3)_2$ (BTBO) was evaluated by the Kurtz–Perry method [32] using a microcrystalline sample synthesized by solid-state reaction and containing a trace amount of BaTiO₃ perovskite. About 50 mg of sieved powder (particle size in the 53-75 µm range) was hand-pressed into a 7 mmdiameter pellet which was irradiated with a pulsed infrared beam (5ns, 10mJ, 10Hz) produced by an optical parametric oscillator pumped by a Nd:YAG laser. A dichroic mirror was used to separate the signal (measured in the reflection mode) from the fundamental and stir the visible light onto a photomultiplier. A combination of a half-wave achromatic retarder and a polarizer was used to control the intensity of the incident power (P_{ω}) , which was measured with a fast IR photodiode. The intensity of the second harmonic signal $(P_{2\omega})$ was fitted to

$$P_{2\omega} = K d_{\rm eff}^2 P_{\omega}^2$$

All the measurements were referred to a sample of $LiNbO_3$ (LNbO) powder (certified reagent from Fisher Scientific, sieved to the same particle size as the BTBO sample). The K factor was taken to be constant



Fig. 2. Mesurement of the powder SHG efficiencies of LiNbO₃ (LNO, top) and Ba₃Ti₃O₆(BO₃)₂ (BTBO, bottom) at a fundamental wavelength (ω) of 1064 nm.

assuming that the BTBO and LNbO samples have similar refractive indices. The absolute SHG efficiency of BTBO was nearly constant within the range of fundamental wavelengths investigated (900–1400 nm). At the wavelength of 1064 nm, the relative efficiency $d_{\rm eff}({\rm BTBO})/d_{\rm eff}({\rm LNbO})$ was determined to be equal to 0.95 ± 0.01 (Fig. 2). This value compares very favorably with the relative efficiencies quoted for other NLO borates, such as LiB₃O₅ (LBO, $d_{\rm eff} = 0.17 \times$ $d_{\rm eff}({\rm LNbO}))$ or BaB₂O₄ (BBO, $d_{\rm eff} = 0.33 \times$ $d_{\rm eff}({\rm LNbO})$) [33].

The large SHG efficiency of BTBO is in agreement with the conclusions of a recent review of NLO properties of inorganic borates [1] where it was found that a common orientation of the anionic BO_3^{3-} groups parallel the polar axis of a non-centrosymmetric crystal structure is favorable for the obtention of large SHG coefficients. This is indeed the case in $Ba_3Ti_3O_6(BO_3)_2$ where all the BO₃ groups have a strictly planar, regular triangular geometry and are parallel to the $\langle 100 \rangle$ and $\langle 110 \rangle$ polar two-fold axes of the structure with only a small misorientation of 3.1° between two adjacent BO₃ groups (Fig. 1). However, apart from the borate groups, the asymmetrical Ti–O bonds in the TiO₆ octahedra (associated with a 0.2 Å off-center displacement of the Ti^{4+} cations) are also expected to contribute significantly to the overall SHG efficiency of BTBO.

 $Ba_3Ti_3O_6(BO_3)_2$ is the first example of a titanium oxoborate with potentially useful NLO properties. Further work is now in progress to improve its synthesis and to investigate the growth of larger single crystals.

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